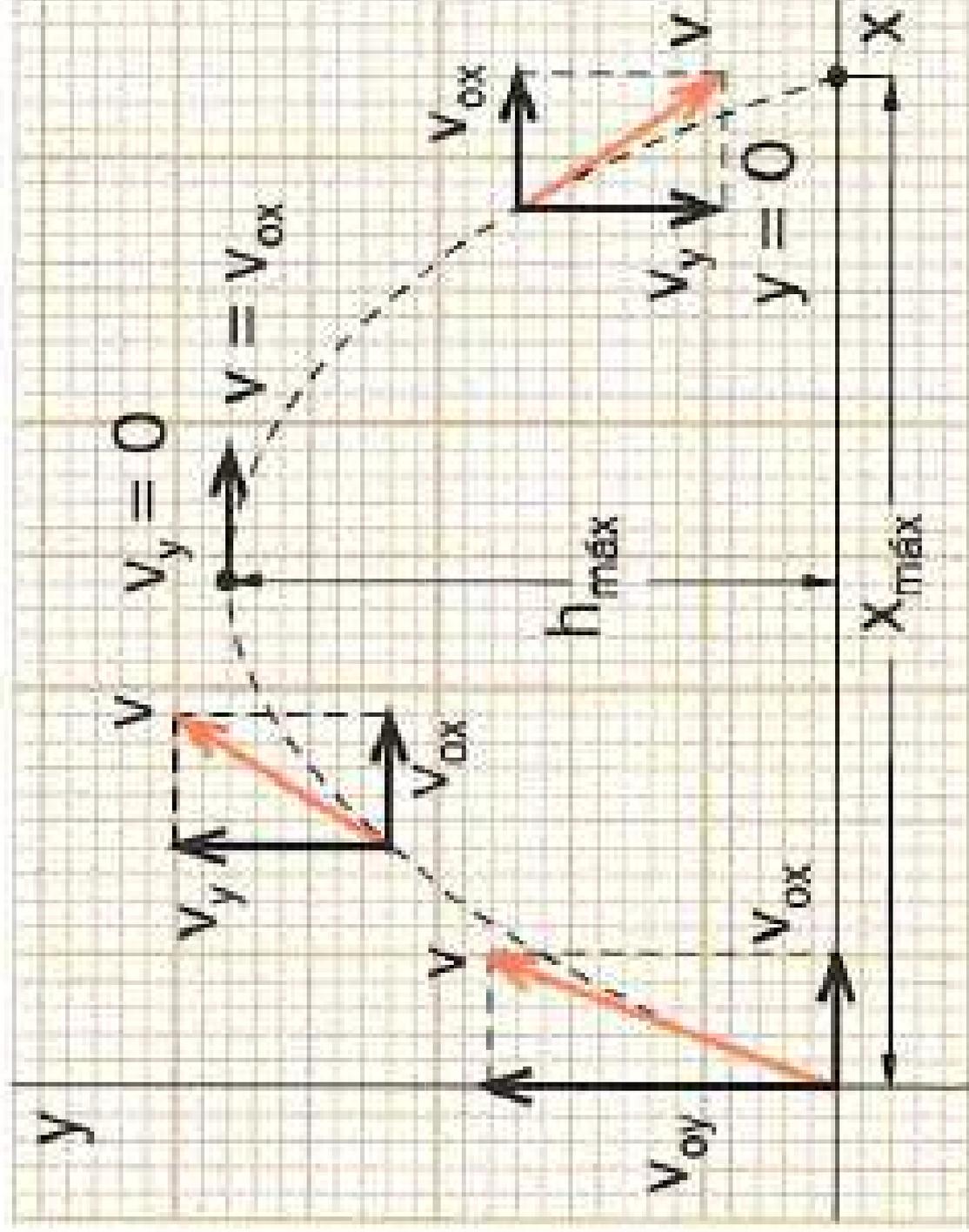
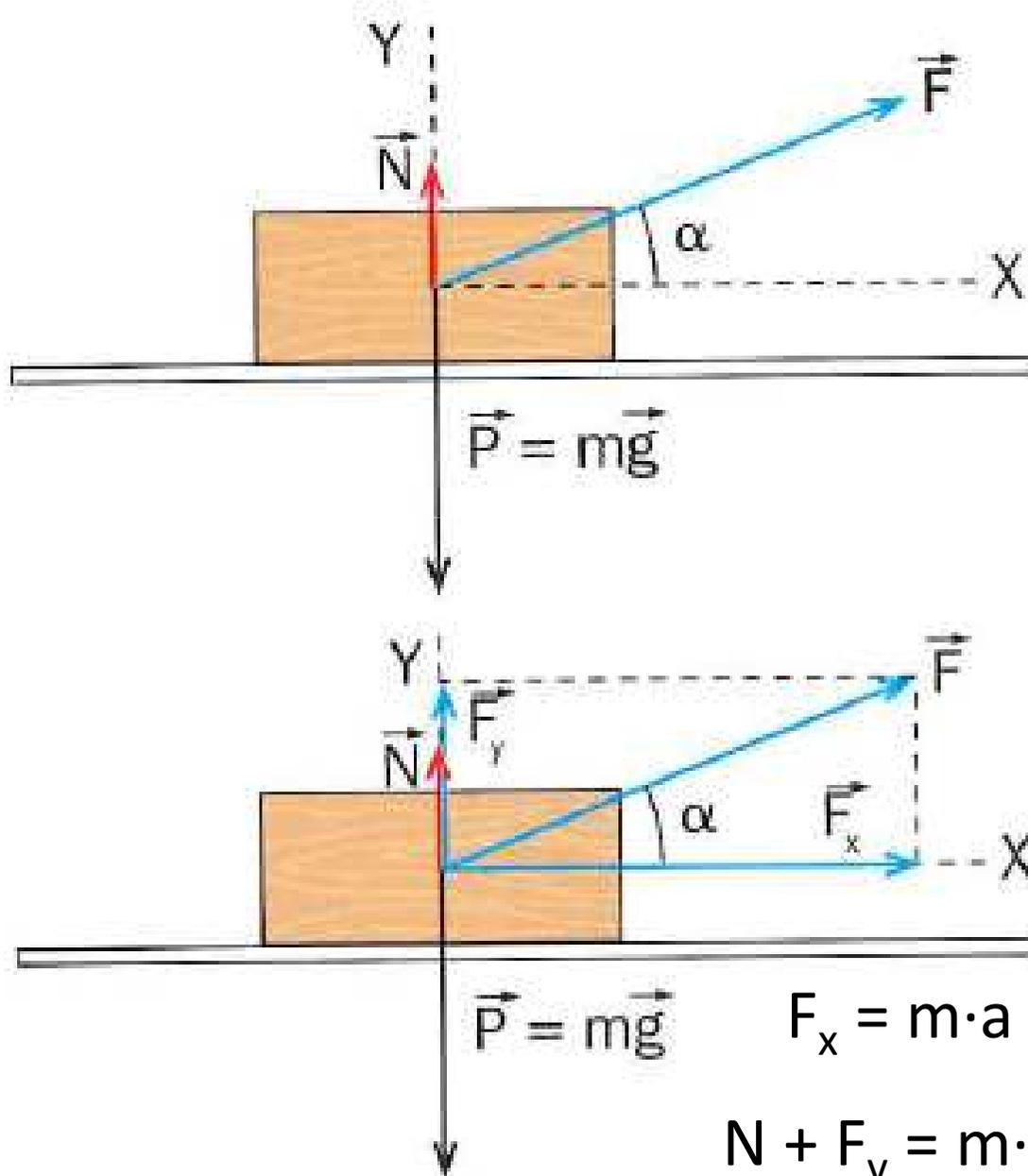


ALTURA MÁXIMA Y ALCANCE



Movimiento sobre un plano horizontal liso

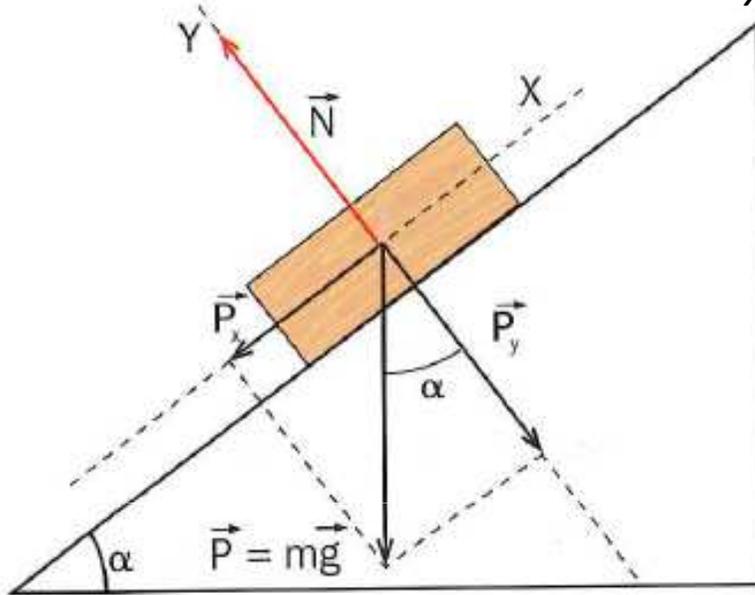


$$F_x = m \cdot a \quad \rightarrow \quad F \cdot \cos \alpha = m \cdot a$$

$$N + F_y = m \cdot g \quad \rightarrow \quad N + F \cdot \sin \alpha = m \cdot g$$

Movimiento sobre un plano inclinado liso

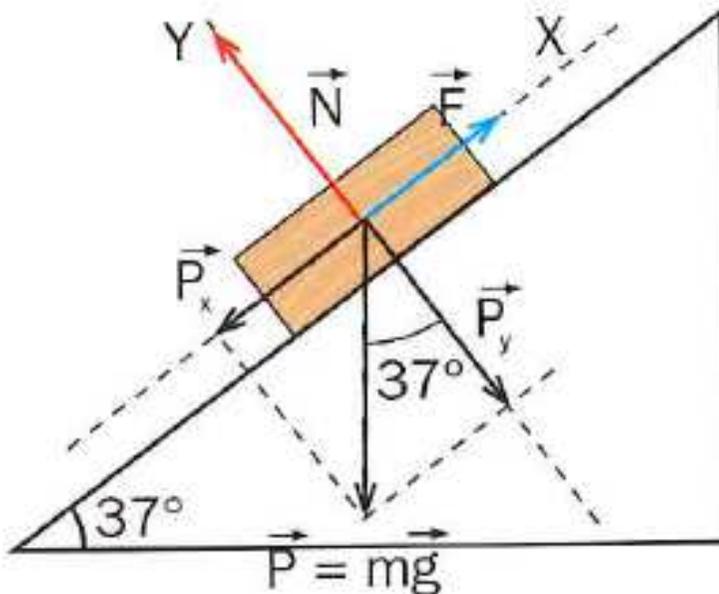
Los ejes de referencia se toman desde la rampa (X) y su perpendicular pasando por el cuerpo



Caída:

$$P_x = m \cdot a \rightarrow mg \cdot \text{sen} \alpha = m \cdot a$$

$$N = P_y \rightarrow N = P \cdot \text{cos} \alpha$$



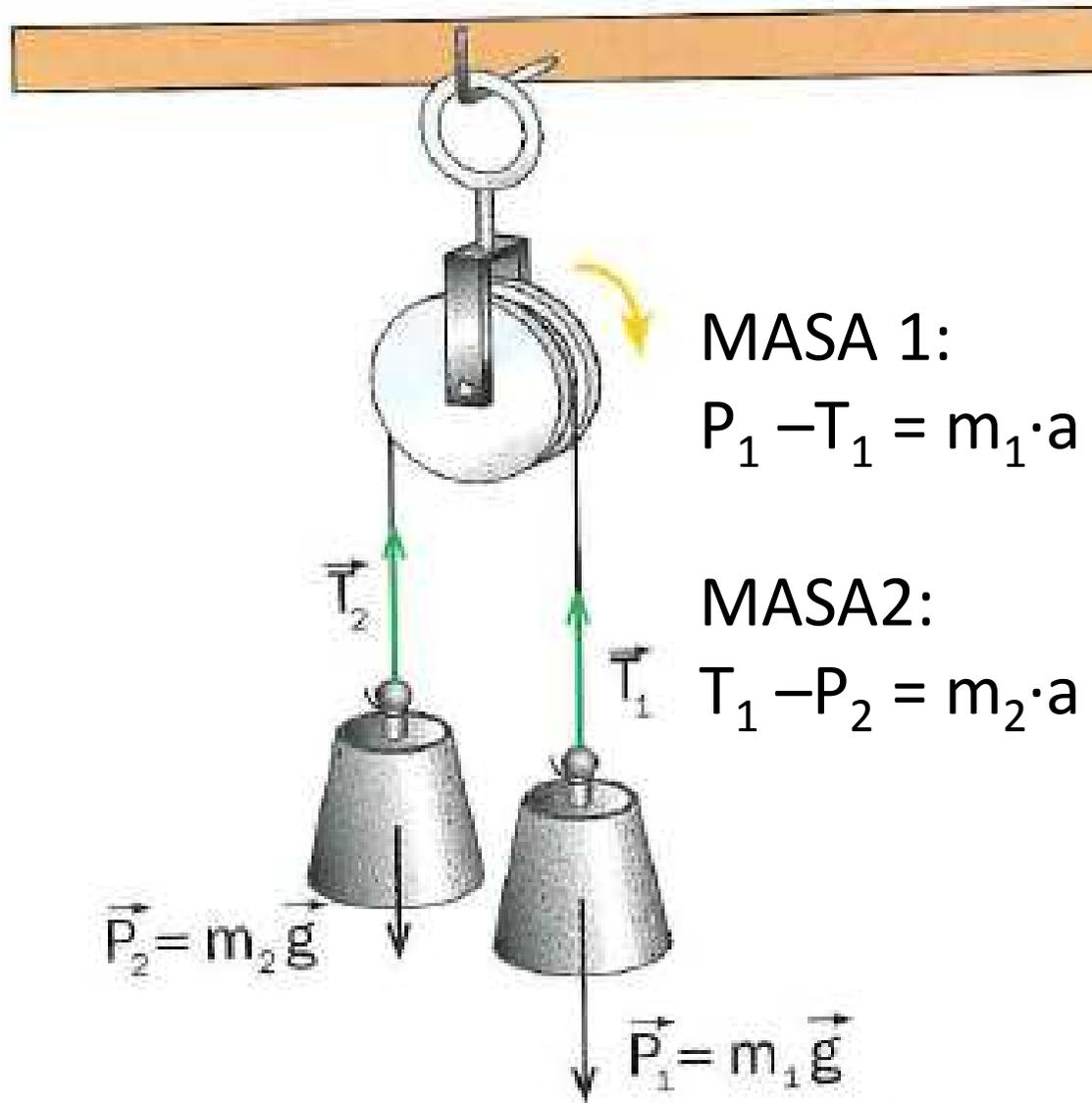
Subida:

$$F - P_x = m \cdot a \rightarrow F - mg \cdot \text{sen} \alpha = m \cdot a$$

$$N = P_y \rightarrow N = P \cdot \text{cos} \alpha$$

■ Cuerpos suspendidos

MÁQUINA DE ATWOOD



MASA 1:

$$P_1 - T_1 = m_1 \cdot a$$

MASA 2:

$$T_1 - P_2 = m_2 \cdot a$$

✓ Las tensiones en ambos lados son iguales:

$$\checkmark T_1 = T_2.$$

✓ Dos masas, por tanto dos veces Newton:

$$m_1 \cdot g - T_1 = m_1 \cdot a$$

$$T_1 - m_2 \cdot g = m_2 \cdot a$$

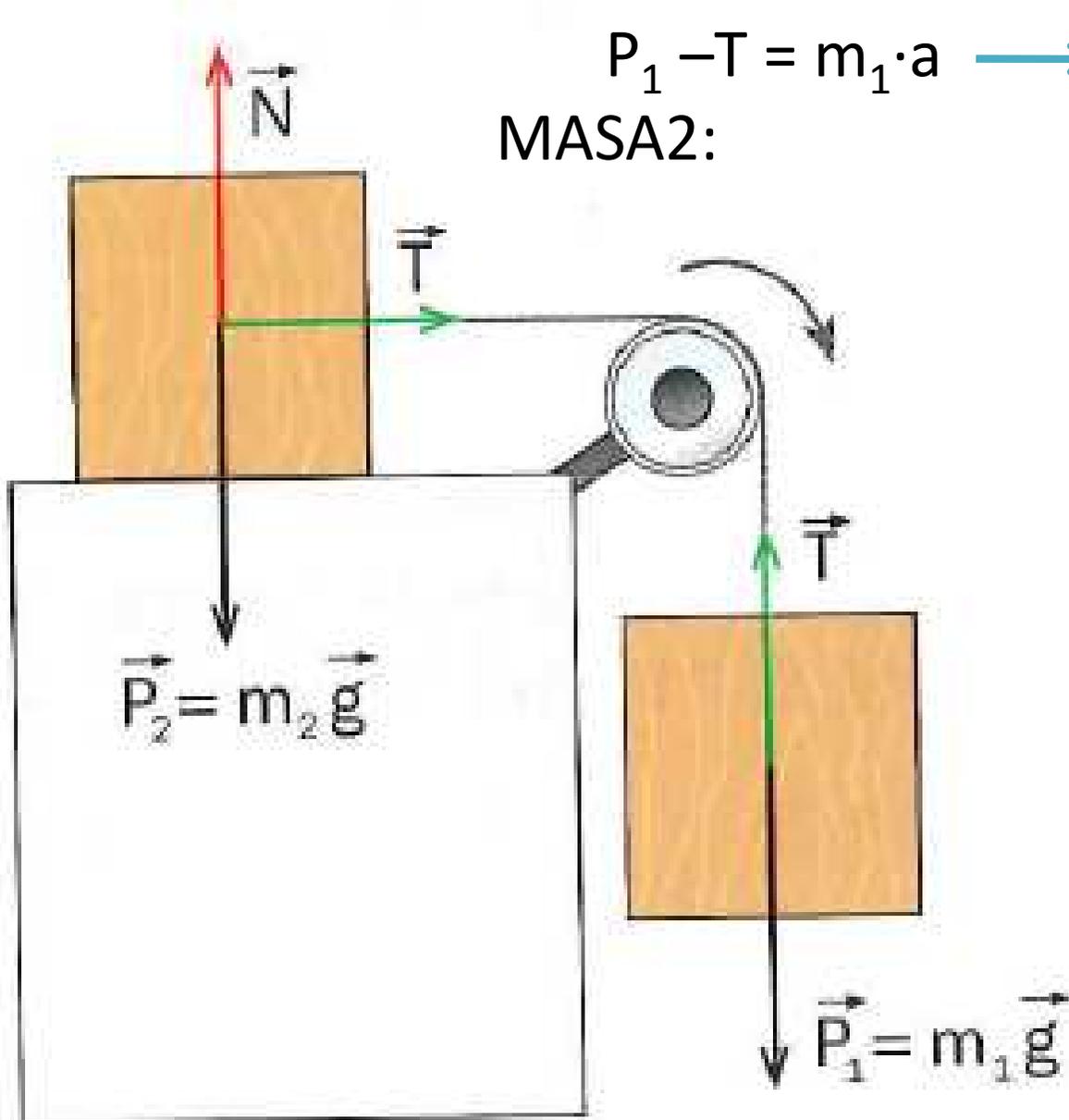
Cuerpos enlazados sobre planos

MASA 1:

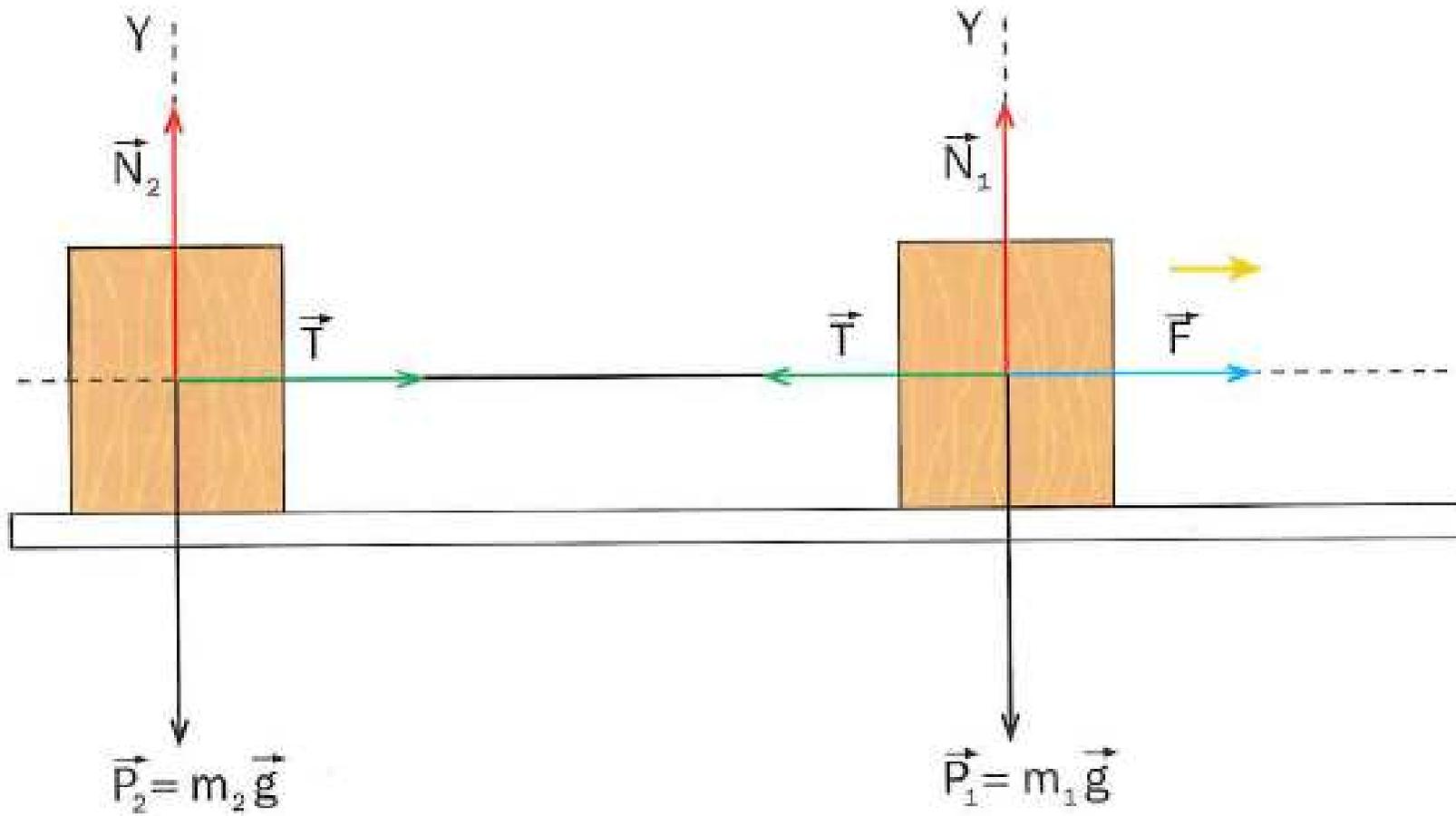
$$P_1 - T = m_1 \cdot a \longrightarrow m_1 \cdot g - T = m_1 \cdot a$$

MASA 2:

$$T = m_2 \cdot a$$



Cuerpos enlazados sobre planos



$$T = m_2 \cdot a$$

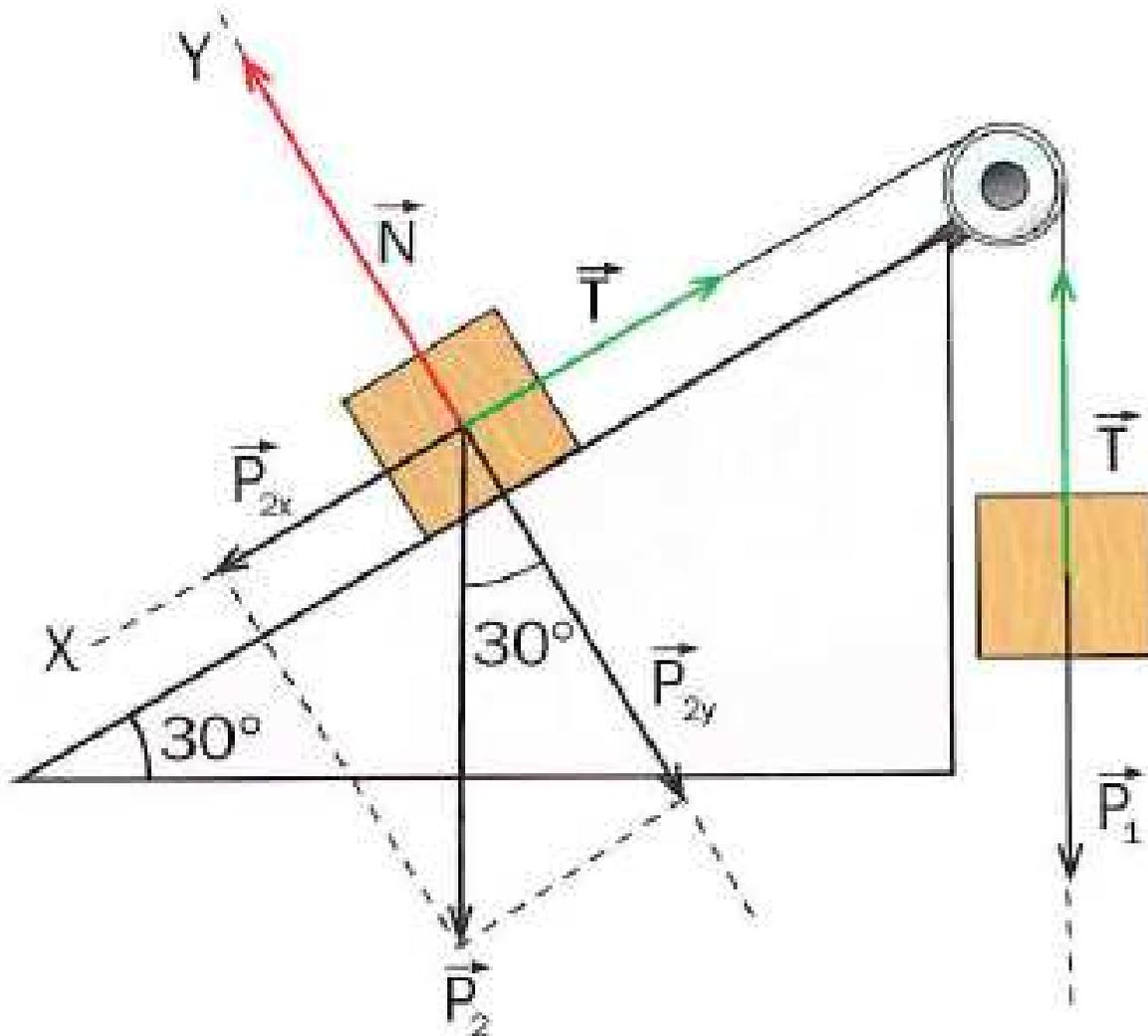
$$F - T = m_1 \cdot a$$

Cuerpos enlazados sobre planos

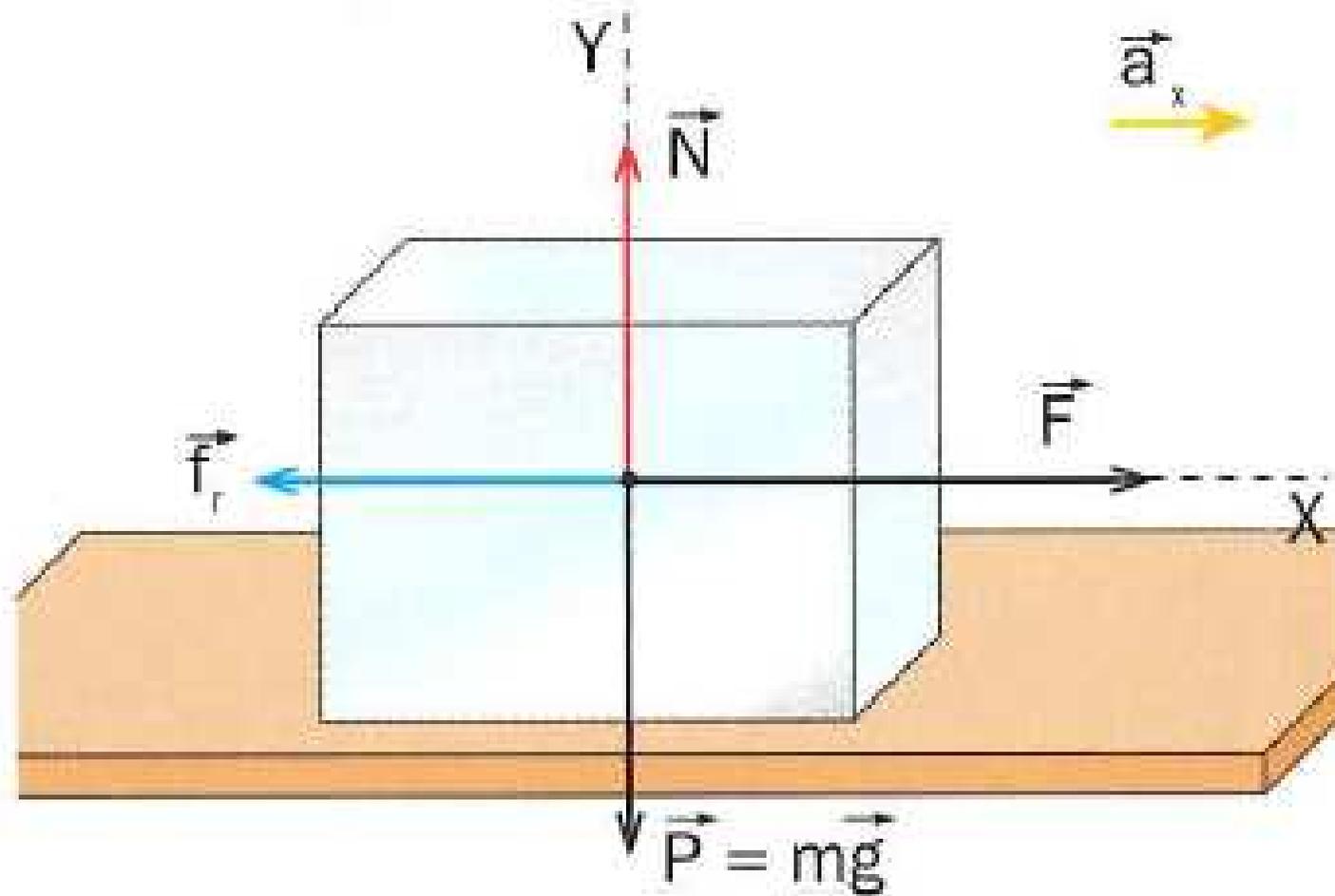
$$T - m_2 \cdot g \cdot \text{sen}30 = m_2 \cdot a$$

Con $N = m_2 \cdot g \cdot \text{cos}30$

$$P_1 - T = m_1 \cdot a$$



Movimiento de cuerpos sobre planos con rozamiento



$$\mathbf{N} = m \cdot g$$

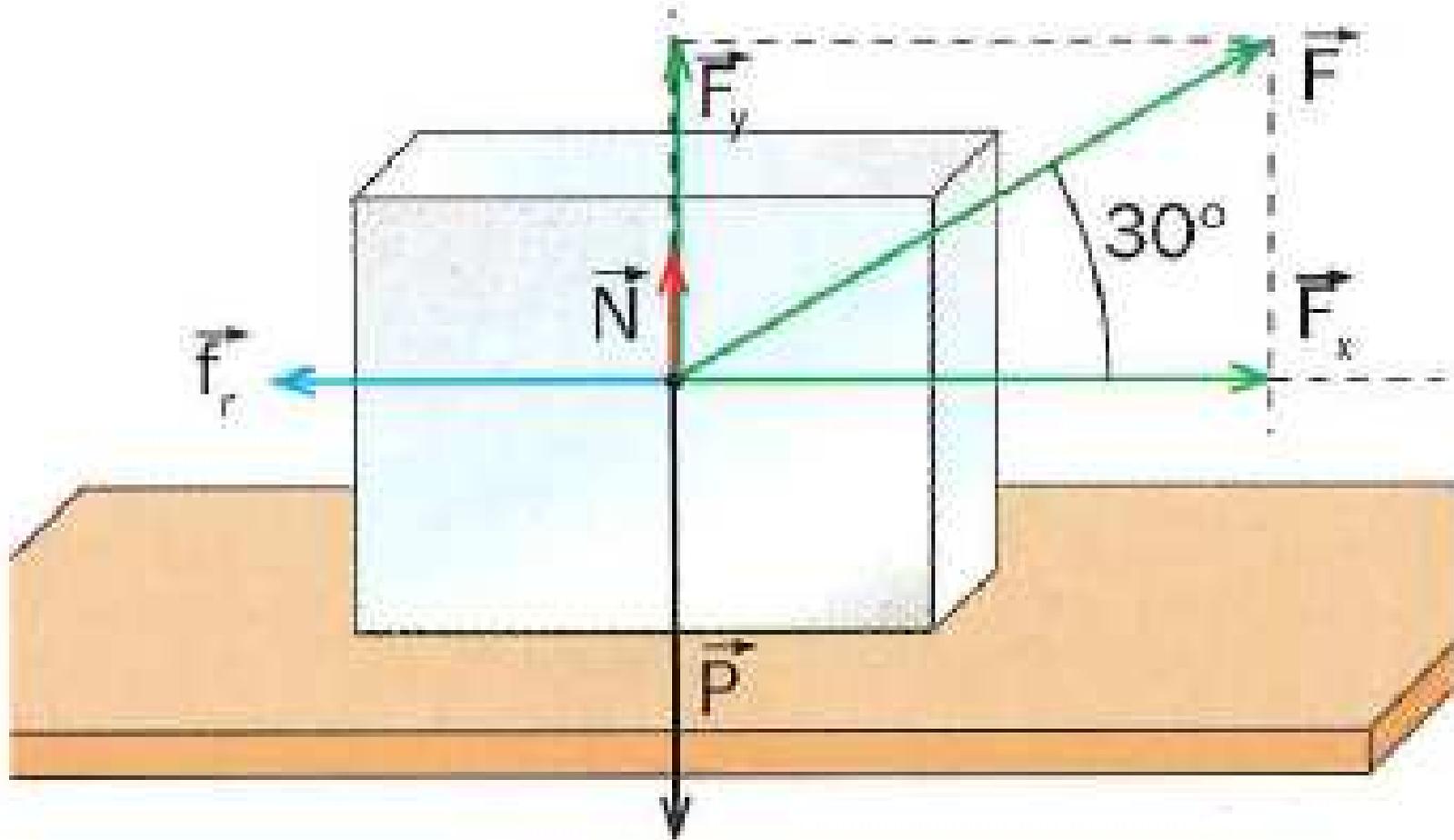
$$\mathbf{f}_r = \mu \cdot \mathbf{N} = \mu \cdot m g \quad \longrightarrow \quad \mathbf{F} - \mu \cdot m g = m \cdot \mathbf{a}$$

Movimiento de cuerpos sobre planos con rozamiento

$$P = N + F_y \longrightarrow N = P - F_y \longrightarrow N = mg - F \cdot \sin 30^\circ ;$$

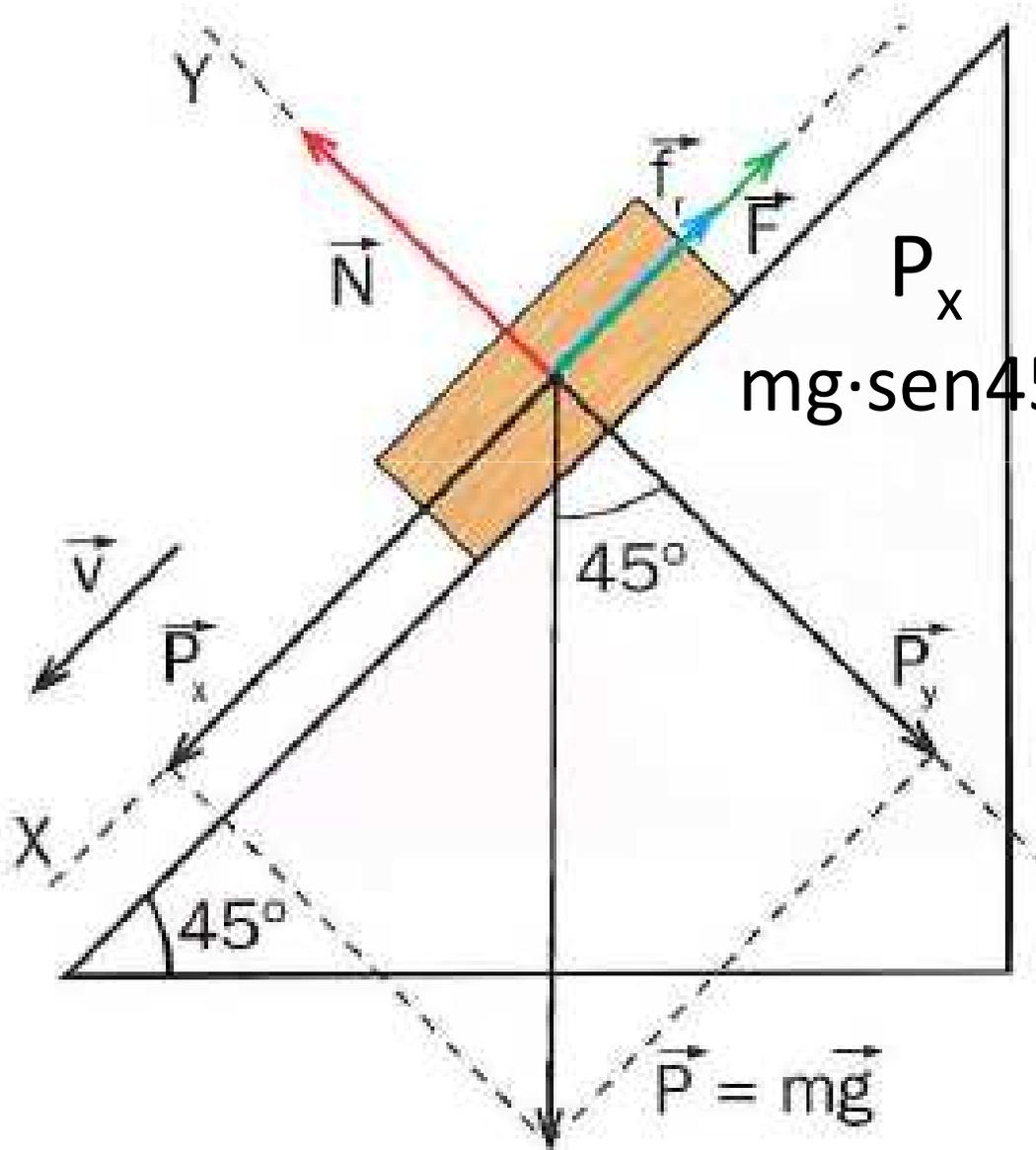
$$f_r = \mu \cdot N = \mu \cdot (mg - F \cdot \sin 30^\circ)$$

$$F_x - f_r = m \cdot a \longrightarrow F \cdot \cos 30^\circ - \mu \cdot (mg - F \cdot \sin 30^\circ) = m \cdot a$$



Movimiento de cuerpos sobre planos con rozamiento

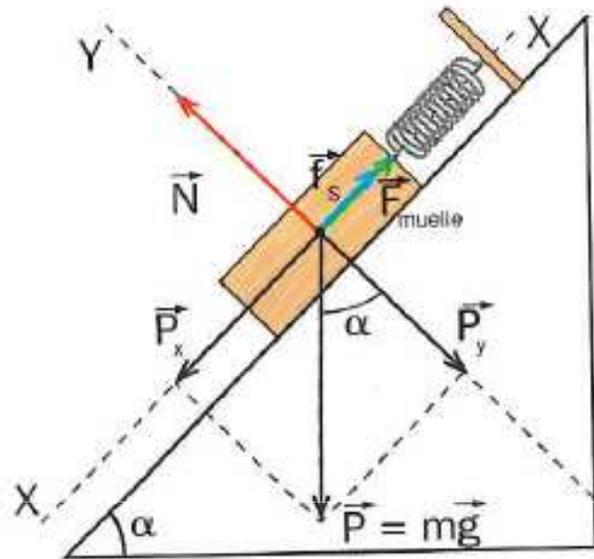
$$\mathbf{N} = P_y \longrightarrow \mathbf{N} = mg \cos 45 \quad f_r = \mu \cdot \mathbf{N} = \mu \cdot mg \cdot \cos 45$$



$$P_x - F - f_r = m \cdot a$$

$$mg \cdot \sin 45 - F - \mu \cdot mg \cdot \cos 45 = m \cdot a$$

Estudio dinámico del movimiento de cuerpos unidos a muelles

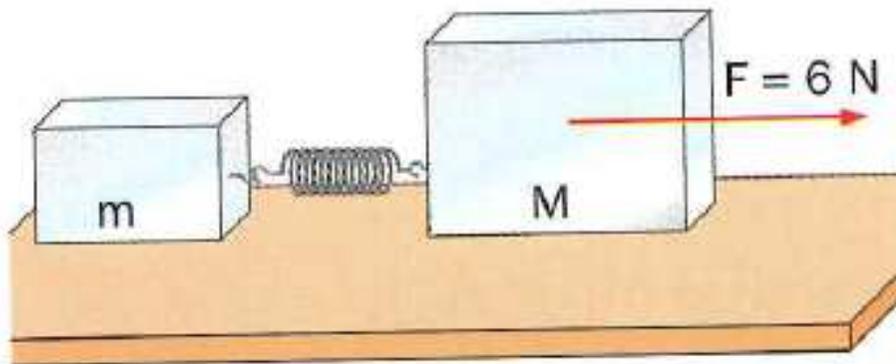


$$P_x - F_{\text{muelle}} - f_r = m \cdot a$$

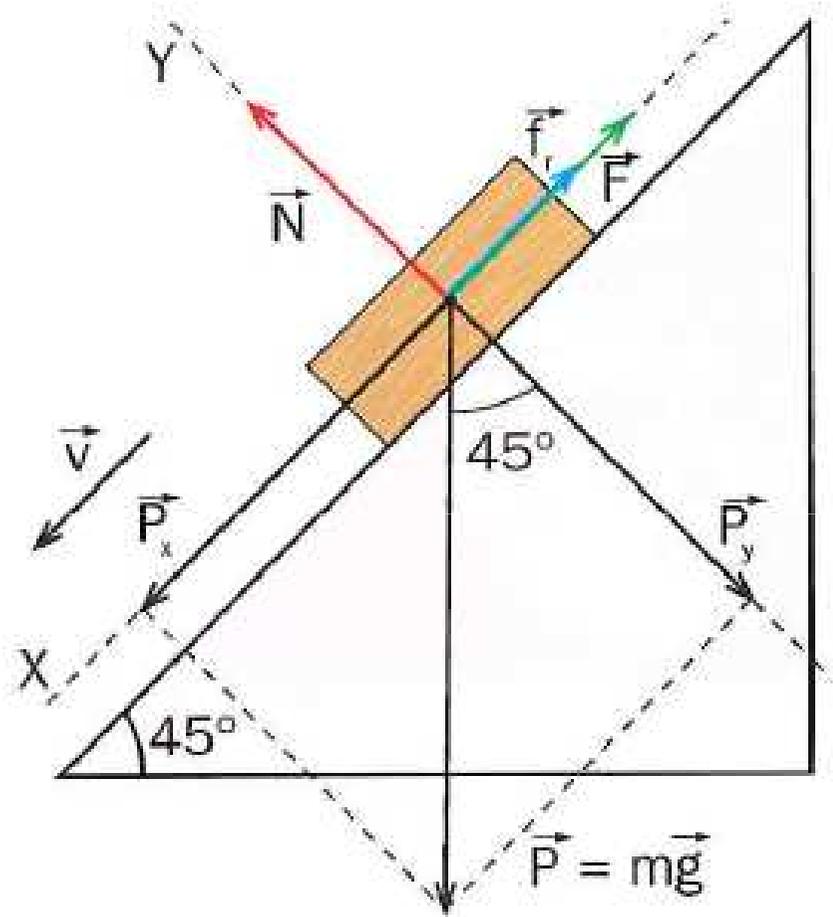
$$mg \sin \alpha - k \cdot x - \mu \cdot mg \cos \alpha = m \cdot a$$

$$F - f_{r1} - F_{\text{muelle}} = M \cdot a$$

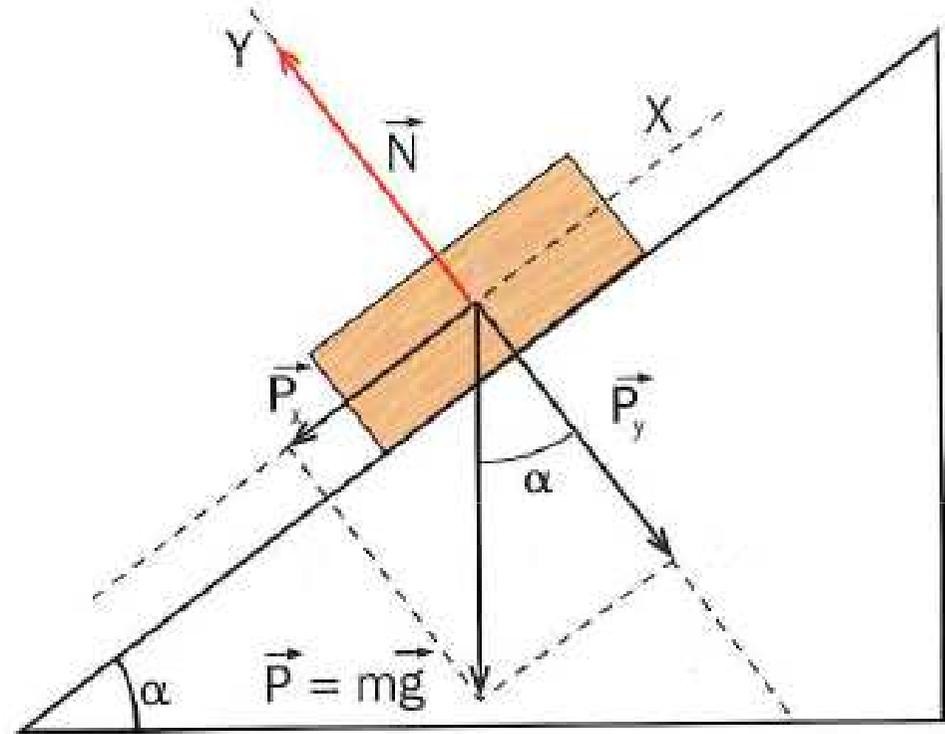
$$F_{\text{muelle}} - f_{r2} = m \cdot a$$



Compara los dos dibujos, ¿Cuál es la diferencia?



$$P_x - F - f_r = m \cdot a$$



$$P_x = m \cdot a$$